## LCOL BASIC SKILLS - PACK 10

## Topics

Differentiation - Can I find the rate of change of a function?
Last Needed - 2022
1 - 2012 LCOL Paper 1 - Question 9 (a)
Complex Numbers - Can I simplify higher powers of $i$ ?
Last Needed - 2021
2013 LCOL Sample Paper 1 - Question 3 (a)
Functions - Can I find the input of a function given its output?
Last Needed - 2023
3 - 2013 LCOL Sample Paper 1 - Question 7 (a)
Statistics - Can I calculate the standard deviation of a set of data?
Last Needed - 2019
4 - 2019 LCOL Paper 2 - Question 7 (c) (ii)
Geometry - Can I use the properties of cyclic quadrilaterals to solve problems?
Last Needed - 2014
5 - 2014 LCOL Sample Paper 2 - Question 6 (b)
www.mathspoints.ie for worked solutions to these questions.
$\square$ LCOL Resources by Topic
$\square$ LCOL Revision - 50 Common Questions

## 1 - 2012 LCOL Paper 1 - Question 9 (a)

Investments can increase or decrease in value. The value of a particular investment of $€ 100$ was found to fit the following model:

$$
V=100+45 t-1.5 t^{2}
$$

where $V$ is the value of the investment in euro, and $t$ is the time in months after the investment was made.
(i) Find the rate at which the value of the investment was changing after 6 months.

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(ii) State whether the value of the investment was increasing or decreasing after 18 months. Justify your answer.

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The investment was cashed in at the end of 24 months.
(iii) How much was it worth at that time?

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## 2 - 2013 LCOL Sample Paper 1 - Question 3 (a)

Write each of the following complex numbers in the form $a+b i$, where $i^{2}=-1$.
$z_{4}=1+i+i^{2}+i^{3}$


3 - 2013 LCOL Sample Paper 1 - Question 7 (a)
Let $h(x)=x^{2}+1$, where $x \in \mathbb{R}$.
Write down a value of $x$ for which $h(x)=50$.

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## 4 - 2019 LCOL Paper 2 - Question 7 (c) (ii)

Table A below shows the price index for thirteen countries in four food categories for the year 2015. (Source: Central Statistics Office.)

It shows, for example, that if you paid $€ 132$ for meat in Austria, then the same quantity of similar meat would cost you € 117 in Germany, $€ 106$ in Ireland, €63 in Lithuania and so on.

The description is the same for the other food categories.

| Table A (€) (Repeat) |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Country | Meat | Fish | Milk, Cheese <br> and Eggs | Fruits, <br> Vegetables <br> and Potatoes |
| Austria | 132 | 125 | 105 | 125 |
| Germany | 117 | 109 | 91 | 111 |
| Ireland | 106 | 108 | 128 | 136 |
| Lithuania | 63 | 73 | 85 | 77 |
| Macedonia | 56 | 59 | 71 | 48 |
| Netherlands | 111 | 99 | 93 | 104 |
| Norway | 157 | 117 | 175 | 150 |
| Poland | 54 | 64 | 65 | 62 |
| Spain | 85 | 89 | 96 | 95 |
| Sweden | 131 | 115 | 116 | 137 |
| Switzerland | 254 | 177 | 148 | 172 |
| Turkey | 78 | 105 | 122 | 86 |
| United Kingdom | 112 | 105 | 118 | 116 |

Use your calculator to find the standard deviation for the data in the Meat category.
Give your answer correct to the nearest whole number.

## Standard deviation:

5 - 2014 LCOL Sample Paper 2 - Question 6 (b)
$A B C D$ is a cyclic quadrilateral.
The opposite sides, when extended, meet at $P$ and $Q$, as shown.

The angles $\alpha, \beta$, and $\gamma$ are as shown.
Prove that $\beta+\gamma=180^{\circ}-2 \alpha$.


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