## LCOL BASIC SKILLS - PACK 7

## Topics

Algebra - Can I solve a simultaneous equation (1 linear equation, 1 non-linear)?
Last Needed - 2021
1-2012 LCOL Paper 1 - Question 3 (b)
Complex Numbers - Can I simplify a complex number expression?
Last Needed - 2023
2 - 2009 LCOL Paper 1 - Question 4 (a)
Area, Perimeter and Volume - Can I calculate the surface areas and volumes of spheres and hemispheres?

Last Needed - 2022
3 - 2006 LCOL Paper 2 - Question 1 (c)
Differentiation - Can I calculate distances, speeds and accelerations using calculus?
Last Needed - 2020
4 - 2011 LCOL Paper 1 - Question 7 (c)
Patterns - Can I find terms of an arithmetic sequence given the formula for the general term?

Last Needed - 2022
5 - 2011 LCOL Paper 1 - Question 3

WWW.mathspoints.ie for worked solutions to these questions.
$\square$ LCOL Resources by Topic
$\square$ LCOL Revision - 50 Common Questions

## 1 - 2012 LCOL Paper 1 - Question 3 (b)

Solve for $x$ and $y$

$$
\begin{aligned}
& x-y+5=0 \\
& x^{2}+y^{2}=17
\end{aligned}
$$

## 2 - 2009 LCOL Paper 1 - Question 4 (a)

Given that $i^{2}=-1$, simplify

$$
2(3-5 i)+7 i(2+3 i)
$$

and write your answer in the form $x+y i$, where $x, y \in \mathbf{R}$.


## 3 - 2006 LCOL Paper 2 - Question 1 (c)

The volume of a hemisphere is $486 \pi \mathrm{~cm}^{3}$.
(i) Find the radius of the hemisphere.

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(ii) Find the volume of the smallest rectangular box that the hemisphere will fit into.


## 4 - 2011 LCOL Paper 1 - Question 7 (c)

A ball is rolled in a straight line along a surface.
The distance, $s$ metres, the ball travels is given by

$$
s=18 t-2 t^{2}
$$

where $t$ is the time in seconds from the instant the ball begins to move.
(i) Find the speed of the ball after 3 seconds.

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(ii) How far is the ball from the starting point when it stops moving?

(iii) Show that the speed of the ball decreases at a constant rate while it is moving.

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5 - 2011 JCHL Paper 1 - Question 3
The terms in an arithmetic sequence are given by the formula $T_{n}=38-4 n$, for $n=1,2,3,4, \ldots$
(a) Write out the first three terms in the sequence.

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(b) What is the first negative term of the sequence.


